#### FORMATIVE ASSESSMENT IN INQUIRY BASED ELEMENTARY MATHEMATICS

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- The international project ASSIST-ME (Assess Inquiry in Science, Technology and Mathematics Education)
- Participants: eight European countries (the Czech Republic, Denmark, Finland, France, Cyprus, Germany, Switzerland and the United Kingdom)
- Objective of research is to develop formative assessment methods that
  - 1. fit into everyday classroom practice,
  - 2. provide qualitatively oriented descriptions and monitoring of competence-oriented, inquiry-based learning processes,
  - 3. can be combined with existing summative assessment requirements and methods used in different educational systems.





#### Specific focus of our research team



**Inquiry based mathematics education (IBME)** "... education which does not present mathematics to pupils and students as a readybuilt structure to appropriate. Rather it offers them the opportunity to experience how mathematical knowledge is developed through personal and collective attempts at answering questions emerging in a diversity of fields, from observation of nature as well as the mathematics field itself, ..." (Artique, Baptist, Dillon, Harlen and Léna 2011, p. 10)

#### **Problem solving competence**

"A task, or goal-directed activity, becomes **a problem** (or problematic) when the "problem solver" ... needs to develop a more productive way of thinking about the given situation." (Lesh and Zawojewski 2007, p. 782)

#### Formative assessment

- Self-assessment
- Peer-assessment



#### Aim of the study



• Questions:

What information teachers and pupils get from formative selfand peer-assessment?

How pupils on primary school level are able to formulate their assessment suggestions for their classmates, understand and accept them?



# The case study - organization



- From October to December 2014
- Two teachers teaching in the  $5^{th}$  grade (children aged 10 11)
  - 8 experimental teaching/learning units
  - the teachers were including IBME where possible
  - To provide space for using methods of formative assessment.
- Topic
  - traditionally taught in this grade of primary school → "great numbers"
- Lesson planning done in cooperation of all members of the local working group in České Budějovice (the authors of this paper and 3 teachers)







- video recordings of the lessons
- audio recordings of group work if it took place
- all pupils' written production was collected
- Worksheets
  - Description of the solving procedure
  - The pupils swapped the worksheets and provided each other with a written feedback on the solving strategies.
  - Having got comments from peers, each pupil (or a group of pupils) had the chance to revise the original solution with respect to the feedback s/he received. In addition, each student also briefly responded in writing to the feedback s/he received.
- Written solutions and comments
  - transcribed
  - open coding





What did the pupils focus on in peer assessment?

- influenced by questions formulated in the worksheet
  - 2<sup>nd</sup> and 3<sup>rd</sup> stages of the solution (quality of the problem solving plan, comprehensibility, clarity of the calculation)
- "in the light" of their own solving procedure
- In the initial stages general comments: "We liked/I did not like"
- Later the comment grew more accurate
- Pupils rarely assessed correctness of the result.



Asproblem: How many lentil grains are there are in a 500 g packaging?

- Initial difficulties in description of the solving procedure
- As the children gradually got more experienced in recording the problems (in the course of sequence of lessons), their comments grew more accurate.

Solvers	Evaluators
First we found out that 5 g contain 80 grains.	We like that they have the
500 : 5 = 100, 100 . 80 = 8 000	same principle as we had.
There should be 8 000 lentil grains in the	😕 But weighing should be
packaging.	accurate.
We poured the grains into a large vessel and	The procedure was correct.
weighed it. We subtracted the mass of the	😕 But our result was different.
vessel from the mass of the grains. We found	
out that the only grains weighed 501 g. Then	
we found out that 20 grains weigh 1 g.	
Calculation: 501.20 = 10 020	





Fig. b

Fig. c

Problem: Record for your friends the manual how to determine the number of small squares on a square grid.

Solvers	Evaluators
Multiple the top row by the vertical row	Their solution is correct. We are not
(from the top to the bottom) and write	quite sure what "number s" stands for.
the result next to the drawing (Fig. a)	We think that the calculated number is
You determined this part (Fig. b)	correct. The description is good.
Now determine the staircase using the	May be everybody would understand.
same procedure (Fig. c)	
Calculate 2 – 5 stairs	Fig. a
2s = 224, 3 s. = 371, 4 s. = 336, 5 s. =	
258	
Now let us add the gained numbers of	
stairs.	
Add this result to number s. That is the	
final result. The result is 1573.	





- As Reactions on assessment "Did your friends' advice help you?"
  - "<sup>(2)</sup> It did not because if they write that the measuring should be accurate, I don't know how exactly".
  - "No. Those who were checking our work must have lost their lentils."
  - "<sup>(C)</sup> Saying the result was different is of no help."
- As the children grew more experience with peer assessment, they grew more self-critical:
  - "We think it should be briefer and we did not finish the manual because we had forgotten." "We think it's all quite muddled." "We could do it better to make it comprehensible. But otherwise we think it's OK."

**Positive influence on the pupils' reasoning.** 



## **Concluding remarks**



Implementation of IBME - impact on the culture of education Using formative assessment contributes to a change of the culture into culture dialogical, sharing, accepting all (even erroneous) ideas.

Peer-assessment

- possible method of assessment, more typical and rooted on Czech primary school level is "on the fly" assessment
- dependent on social climate in the classroom
- Influence of pupils' experience in it
- the criteria for assessment
  - first formulated by the teacher according to educational objectives
  - if the criteria are formulated on a very general level, the pupils will discover some criteria on their own



### **Concluding remarks**



Our research of formative assessment in IBME will continue – two rounds of testing are planned for 2015 (geometry, prealgebraic thinking).

- deeper a priori analysis and more accurate formulation of the goal of the teaching/learning experiments and of the problems solved by the pupils
- development of more detailed criteria of assessment.
  "On-the-fly formative assessment arises when a "teachable moment" unexpectedly occurs, for example, when a teacher circulating and listening to the conversation among students in small groups overhears a students say ... (Shavelson et al., 2008, p.300).





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